## COSC170 - Compiler Construction Homework 1

Due: 2009 Feb 06, beginning of lecture

1. Draw the finite state machines, and write regular expressions that denote the strings recognized by the following finite automata:
(a) $s_{1}$ is the start state; $s_{2}$ is the final (accepting) state

|  | $a$ | $b$ |
| :---: | :---: | :---: |
| $s_{1}$ |  | $s_{2}$ |
| $s_{2}$ | $s_{3}$ |  |
| $s_{3}$ |  | $s_{2}$ |

(b) $s_{1}$ is the start state; $s_{4}$ is the final state

|  | $a$ | $b$ |
| :---: | :---: | :---: |
| $s_{1}$ | $s_{2}$ | $s_{3}$ |
| $s_{2}$ |  | $s_{4}$ |
| $s_{3}$ | $s_{4}$ |  |
| $s_{4}$ |  | $s_{4}$ |

(c) $s_{1}$ is both the start state and the final state

|  | $a$ | $b$ | $c$ |
| :---: | :---: | :---: | :---: |
| $s_{1}$ | $s_{2}$ | $s_{3}$ | $s_{4}$ |
| $s_{2}$ | $s_{1}$ |  |  |
| $s_{3}$ |  | $s_{1}$ |  |
| $s_{4}$ |  |  | $s_{1}$ |

(d) $s_{1}$ is the start state; $s_{1}$ and $s_{3}$ are final states

|  | $a$ | $b$ | $c$ |
| :---: | :---: | :---: | :---: |
| $s_{1}$ | $s_{2}$ |  |  |
| $s_{2}$ |  | $s_{2}$ | $s_{3}$ |
| $s_{3}$ |  |  |  |

2. Write DFA's that recognize the following languages. Be careful to note starting and accepting states in your automata.
(a) $\left\{w \in\{a, b\}^{*}:\right.$ each $a$ in $w$ is followed by at least one $\left.b\right\}$
(b) $\left\{w \in\{a, b\}^{*}: w\right.$ contains precisely three $a$ 's $\}$
(c) $\left\{w \in\{a, b\}^{*}: w\right.$ has an odd number of $a$ 's and an even number of $b$ 's $\}$
(d) $\left\{w \in\{a, b\}^{*}: w\right.$ has bab as a substring $\}$
3. Consider the following regular expression:

$$
\left(a b c^{*} \mid a^{*} b c\right)
$$

(a) As described in class, construct an NFA for this expression.
(b) Using subset construction, convert the NFA into a DFA.
(c) Optimize the DFA to minimize the number of states.
4. Consider the grammar below:

(a) Write a grammar that accepts the same language as the grammar above, but that is suitable for LL(1) parsing.
(b) Find FIRST and FOLLOW sets for your grammar.
(c) Show the LL(1) parsing table for your grammar.
(d) Given the input string, "x $=5$; print $(x, 6)$ ", use your parse table to expand the goal into a parse for the expression. Note which grammar production is applied at each step.

